

1. A method of identifying a user, comprising the steps of:

a) selecting a modulus  $p$  from the group of equations consisting of:

$$p=(2^{dk}-2^{ck}-1)/r,$$

where  $0<2c\leq d$ , where  $r \neq 1$ , and where  $GCD(c,d)=1$ ;

$$p=(2^{dk}-2^{(d-1)k}+2^{(d-2)k}-\dots-2^k+1)/r,$$

where  $d$  is even, and where  $k$  is not equal to 2 (mod 4);

$$p=(2^{dk}-2^{ck}-1)/r,$$

where  $3d<6c<4d$ , and where  $GCD(c,d)=1$ ;

$$p=(2^{dk}-2^{ck}+1)/r,$$

where  $0<2c\leq d$ , where  $r \neq 1$ , and where  $GCD(c,d)=1$ ; and

$$p=(2^{4k}-2^{3k}+2^{2k}+1)/r;$$

b) selecting an elliptic curve  $E$  and an order  $q$ ;

c) selecting a basepoint  $G$ ;

- d) generating a private key  $w$ ;
- e) generating a public key  $W=wG$ ;
- f) distributing  $p$ ,  $E$ ,  $q$ ,  $G$ , and  $W$  in an authentic manner;
- g) retrieving, by a prover, the prover's private key  $w$ ;
- h) retrieving, by a verifier, the prover's public key  $W$ ;
- i) generating, by the prover, a private integer  $k$ ;
- j) combining, by the prover,  $k$  and the prover's  $G$  to form  $K$  using the form of the prover's

modulus  $p$ ;

- k) sending, by the prover,  $K$  to the verifier;
- l) sending, by the verifier, a challenge integer  $c$  to prover;
- m) combining, by the prover,  $c$ ,  $k$ , and  $w$  to form a response integer  $v$ ;
- n) sending, by the prover,  $v$  to the verifier; and
- o) combining, by the verifier,  $cG$ ,  $K$ , and  $W$  using the form of the prover's modulus  $p$  and checking to see if the combination is equal to  $vG$ , if so the user is identified as the user, otherwise the user is not identified as the user.

2. A method of generating a digital signature, comprising the steps of:

- a) selecting a modulus  $p$  from the group of equations consisting of:

$$p=(2^{dk}-2^{ck}-1)/r,$$

where  $0 < 2c \leq d$ , where  $r \neq 1$ , and where  $GCD(c, d) = 1$ ;

$$p=(2^{dk}-2^{(d-1)k}+2^{(d-2)k}-\dots-2^k+1)/r,$$

where  $d$  is even, and where  $k$  is not equal to 2 (mod 4);

$$p=(2^{dk}-2^{ck}-1)/r,$$

where  $3d < 6c < 4d$ , and where  $GCD(c, d)=1$ ;

$$p=(2^{dk}-2^{ck}+1)/r,$$

where  $0 < 2c \leq d$ , where  $r \neq 1$ , and where  $GCD(c, d)=1$ ; and

$$p=(2^{4k}-2^{3k}+2^{2k}+1)/r;$$

- b) selecting an elliptic curve  $E$  and an order  $q$ ;
- c) selecting a basepoint  $G$ ;
- d) generating a private key  $w$ ;
- e) generating a public key  $W=wG$ ;
- f) distributing  $p$ ,  $E$ ,  $q$ ,  $G$ , and  $W$  in an authentic manner;
- g) retrieving, by a signer, the signer's private key  $w$ ;
- h) generating, by the signer, a private integer  $k$ ;
- i) combining, by the signer,  $k$  and  $G$  to form  $K$  using the form of the prover's modulus  $p$ ;
- j) combining, by the signer,  $K$  and a message  $M$  to form an integer  $h$ ;

- k) combining by the signer,  $h$ ,  $k$ , and  $w$  to form an integer  $s$ ; and
- l) sending, by the signer,  $M$  and  $(K,s)$  as a digital signature of  $M$ .

3. The method of claim 1, further including the steps of:

- a) retrieving, by the verifier, the prover's public key  $W$ ;
- b) receiving, by the verifier,  $M$  and  $(K,s)$ ;
- c) combining, by the verifier,  $K$  and  $M$  to form an integer  $h$ ; and
- d) combining, by the verifier,  $h$ ,  $k$ , and  $W$  using the form of the prover's modulus  $p$  and

checking to see if the combination is equal to  $sG$ , if so then the digital signature is verified, otherwise the digital signature is not verified.

4. A method of generating a digital signature, comprising the steps of:

- a) selecting a modulus  $p$  from the group of equations consisting of:

$$p=(2^{dk}-2^{ck}-1)/r,$$

where  $0 < 2c \leq d$ , where  $r \neq 1$ , and where  $GCD(c,d)=1$ ;

$$p=(2^{dk}-2^{(d-1)k}+2^{(d-2)k}-\dots-2^k+1)/r,$$

where  $d$  is even, and where  $k$  is not equal to 2 (mod 4);

$$p=(2^{dk}-2^{ck}-1)/r,$$

where  $3d < 6c < 4d$ , and where  $GCD(c, d) = 1$ ;

$$p = (2^{dk} - 2^{ck} + 1)/r,$$

where  $0 < 2c \leq d$ , where  $r \neq 1$ , and where  $GCD(c, d) = 1$ ; and

$$p = (2^{4k} - 2^{3k} + 2^{2k} + 1)/r;$$

- b) selecting an elliptic curve  $E$  and an order  $q$ ;
- c) selecting a basepoint  $G$ ;
- d) generating a private key  $w$ ;
- e) generating a public key  $W = wG$ ;
- f) distributing  $p$ ,  $E$ ,  $q$ ,  $G$ , and  $W$  in an authentic manner;
- g) retrieving, by a signer, the signer's private key  $w$ ;
- h) generating, by the signer, a private integer  $k$ ;
- i) combining, by the signer,  $k$  and  $G$  to form  $K$  using the form of the prover's modulus  $p$ ;
- j) combining, by the signer,  $K$  and a message  $M$  to form an integer  $h$ ;
- k) combining by the signer,  $h$ ,  $k$ , and  $w$  to form an integer  $s$ ; and
- l) sending, by the signer,  $M$  and  $(h, s)$  as a digital signature of  $M$ .

5. The method of claim 4, further including the steps of:

- a) retrieving, by the verifier, the prover's public key  $W$ ;

- b) receiving, by the verifier,  $M$  and  $(h,s)$ ;
- c) combining, by the verifier,  $h$ ,  $W$ , and  $sG$  using the form of the prover's modulus  $p$  to form  $K$ ;
- d) combining, by the verifier,  $K$  and  $M$  to form an integer  $h'$ ; and
- e) checking, by the verifier, that  $h$  is equal to  $h'$ , if so then the digital signature is verified, otherwise the digital signature is not verified.